

$$\begin{array}{ll}
\varsigma \in \Sigma = \mathbf{Call} \times \mathit{BEnv} \times \mathit{VEnv} \times \mathit{Time} & \hat{\varsigma} \in \hat{\Sigma} = \mathbf{Call} \times \widehat{\mathit{BEnv}} \times \widehat{\mathit{VEnv}} \times \widehat{\mathit{Time}} \\
\beta \in \mathit{BEnv} = \mathbf{Var} \rightarrow \mathit{Bind} & \hat{\beta} \in \widehat{\mathit{BEnv}} = \mathbf{Var} \rightarrow \widehat{\mathit{Bind}} \\
ve \in \mathit{VEnv} = \mathit{Bind} \rightarrow \mathit{D} & \hat{ve} \in \widehat{\mathit{VEnv}} = \widehat{\mathit{Bind}} \rightarrow \hat{\mathit{D}} \\
d \in \mathit{D} = \mathit{Val} & \hat{d} \in \hat{\mathit{D}} = \mathcal{P}(\widehat{\mathit{Val}}) \\
val \in \mathit{Val} = \mathit{Clo} & \hat{val} \in \widehat{\mathit{Val}} = \widehat{\mathit{Clo}} \\
clo \in \mathit{Clo} = \mathbf{Lam} \times \mathit{BEnv} & \hat{clo} \in \widehat{\mathit{Clo}} = \mathbf{Lam} \times \widehat{\mathit{BEnv}} \\
b \in \mathit{Bind} \text{ is an \textbf{infinite} set of bindings} & \hat{b} \in \widehat{\mathit{Bind}} \text{ is a \textbf{finite} set of bindings} \\
t \in \mathit{Time} \text{ is an \textbf{infinite} set of times} & \hat{t} \in \widehat{\mathit{Time}} \text{ is a \textbf{finite} set of times}
\end{array}$$

Fig. 1. State-space for the lambda calculus: Concrete (left) and abstract (right).

we can define the single concrete transition rule for CPS:

$$\begin{aligned}
& \llbracket (f \ e_1 \dots e_n)^\ell \rrbracket, \beta, ve, t \Rightarrow (call, \beta'', ve', t'), \text{ where:} \\
& d_i = \mathcal{E}(e_i, \beta, ve) \\
& d_0 = \llbracket (\lambda^{\ell'} (v_1 \dots v_n) \ call) \rrbracket, \beta' \\
& t' = tick(call, t) \\
& b_i = alloc(v_i, t') \\
& \beta'' = \beta'[v_i \mapsto b_i] \\
& ve' = ve[b_i \mapsto d_i].
\end{aligned}$$

With the help of an abstract evaluator, $\hat{\mathcal{E}} : \mathbf{Exp} \times \widehat{\mathit{BEnv}} \times \widehat{\mathit{VEnv}} \rightarrow \hat{\mathit{D}}$:

$$\begin{aligned}
\hat{\mathcal{E}}(v, \hat{\beta}, \hat{ve}) &= \hat{ve}(\hat{\beta}(v)) \\
\hat{\mathcal{E}}(lam, \hat{\beta}, \hat{ve}) &= \{(lam, \hat{\beta})\},
\end{aligned}$$

we can define an analogous transition rule for the abstract semantics:

$$\begin{aligned}
& \llbracket (f \ e_1 \dots e_n)^\ell \rrbracket, \hat{\beta}, \hat{ve}, \hat{t} \rightsquigarrow (call, \hat{\beta}'', \hat{ve}', \hat{t}'), \text{ where:} \\
& \hat{d}_i = \hat{\mathcal{E}}(e_i, \hat{\beta}, \hat{ve}) \\
& \hat{d}_0 \ni \llbracket (\lambda^{\ell'} (v_1 \dots v_n) \ call) \rrbracket, \hat{\beta}' \\
& \hat{t}' = \widehat{tick}(call, \hat{t}) \\
& \hat{b}_i = \widehat{alloc}(v_i, \hat{t}') \\
& \hat{\beta}'' = \hat{\beta}'[v_i \mapsto \hat{b}_i] \\
& \hat{ve}' = \hat{ve} \sqcup [\hat{b}_i \mapsto \hat{d}_i].
\end{aligned}$$