If $g(b)$ and $g(b')$ are reachable and $\alpha(b) = \alpha(b')$, then $b = b'$.